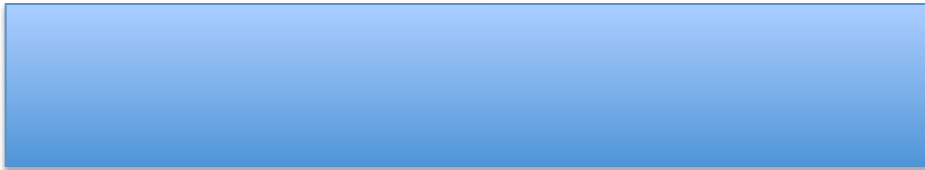
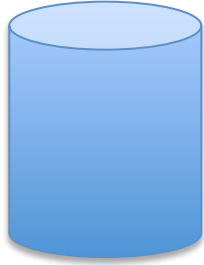


If we cover a pocket radio with an aluminum mesh



1. Nothing happens
2. Sound gets louder
3. Sound gets quieter
4. None of the above

$\frac{1}{1} = \frac{1}{3} + \frac{1}{x}$

$\frac{1}{C_2} = \frac{1}{C_1} + \frac{1}{C_3}$

$\frac{1}{4} = \frac{1}{3} + \frac{1}{C_2}$

$\frac{1}{4} - \frac{1}{3} = \frac{1}{C_2}$

$\frac{3-4}{12} = \frac{1}{C_2}$

$\frac{-1}{12} = \frac{1}{C_2}$

$C_2 = -12$

$C_2$  add to  $3 \mu F \Rightarrow C_{eq} = 1 \mu F$

1.  $2 \mu F$
2.  $4 \mu F$
3.  $0.666 \mu F$
4.  $1.5 \mu F$
5. Imp.

$$\frac{1}{1} = \frac{1}{3} + \frac{1}{X} \quad X = 0.66$$

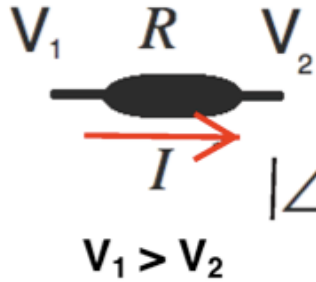
$$\frac{3 \cdot 1}{3 \cdot 1} - \frac{1}{3} = \frac{1}{X}$$

$$\frac{3-1}{3} = \frac{1}{X}$$

$$\frac{2}{3} = \frac{1}{X}$$

$$\frac{X}{1} = \frac{3}{2} = 1.5$$

# Ohm's Law, Resistance, Resistivity



This is what we have proved:

$$|\Delta V| = V_1 - V_2 = IR > 0$$
$$I = \frac{|\Delta V|}{R} = \frac{|\Delta V|}{\left(\rho \frac{l}{A}\right)}$$

$$I = \frac{|\Delta V|}{R} \quad \text{or} \quad |\Delta V| = R I$$

This equation is called the **Ohm's Law**.

According to the Ohm's Law:

*current and potential difference are directly proportional.*

The variable  $R$  is called *Resistance* (of a wire, of a device, of a bulb, of a motor, etc.).

*Resistance* of a wire is directly proportional to its length  $l$  and inversely proportional to its cross-sectional area  $A$  : the variable  $\rho$  is called *Resistivity* of the material (the metal the wire is

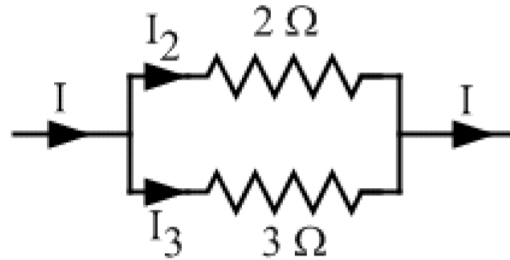
made of):

$$R = \rho \frac{l}{A}$$

# The junction rule

A junction is a place where three or more current paths meet.

The junction rule: **The total current coming into a junction equals the total current going out from a junction.**



In the picture, a  $2\ \Omega$  resistor is in parallel with a  $3\ \Omega$  resistor. A current  $I$  comes into the junction before the resistors, splitting into two currents  $I_2$  through the  $2\ \Omega$  resistor and  $I_3$  through the  $3\ \Omega$  resistor.

The junction rule tells us that  $I = I_2 + I_3$

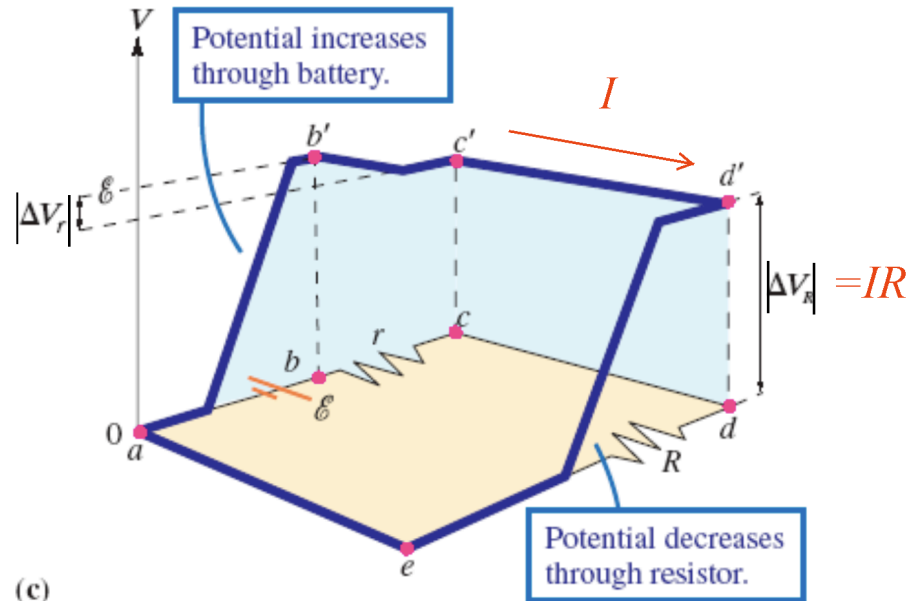
The sum of all the potential differences around a closed loop equals zero.

$$\sum \Delta V = 0 \quad \text{for a complete loop}$$

## Loop Rule

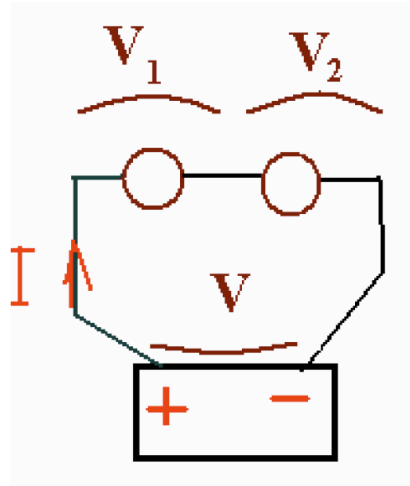
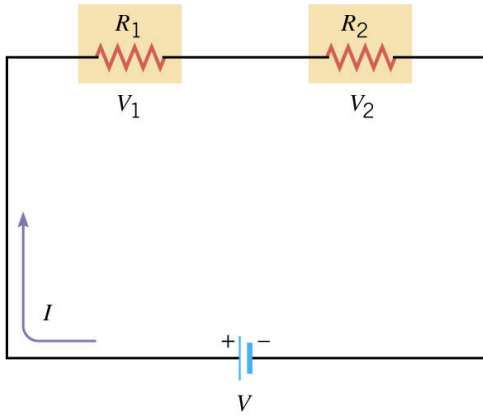
$r = 10 \text{ Ohm}$ ,  $R = 20 \text{ Ohm}$ ,  $I = 0.1 \text{ A}$ .  
Let's find all the potentials.

Basic single-loop circuit:



Current  $I$  is the same!

$$V = V_1 + V_2 = \underline{I}R_1 + \underline{I}R_2 = I(R_1 + R_2) = IR_S$$



*Series resistors*

$$R_S = R_1 + R_2 + R_3 + \dots$$

**$R_S$  is equivalent resistance**

## Parallel Wiring

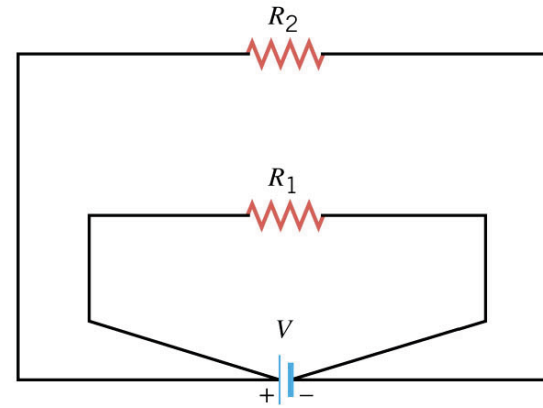
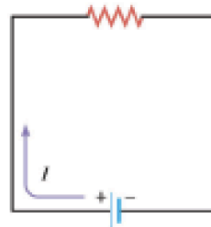
Ohm's  
Law

$$I = I_1 + I_2 = \frac{V}{R_1} + \frac{V}{R_2} = V \left( \frac{1}{R_1} + \frac{1}{R_2} \right) = V \left( \frac{1}{R_p} \right)$$

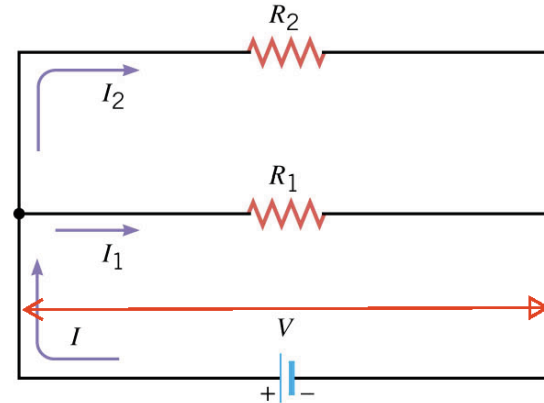
**parallel resistors**

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$$

**$R_p$  is equivalent resistance**



(a)



(b)



# Electric Power

The work done by the current on a device is equal to the energy spent to carry the charge through the device.

$$\underline{W = U = Q \cdot \Delta V = I \cdot \Delta V \cdot \Delta t}$$

By a definition: Power = work/time

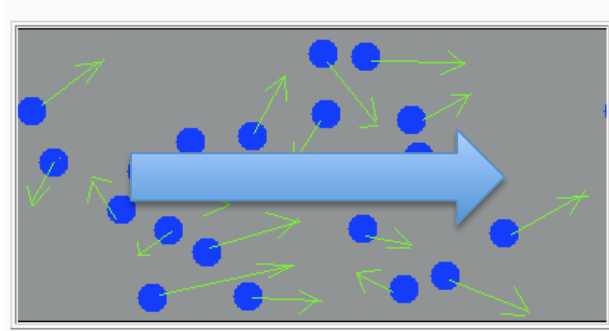
$$P = \frac{W}{\Delta t} = \frac{I \cdot \Delta V \cdot \Delta t}{\Delta t} = I \cdot \Delta V$$

If we use the Ohm's Law ( $\Delta V = I \cdot R$ ), we can get other expressions:

$$P = I \cdot \Delta V = I^2 \cdot R = \frac{(\Delta V)^2}{R}$$

The unit for power is Amp\*V = W (Watt)

## Conductor in electric field

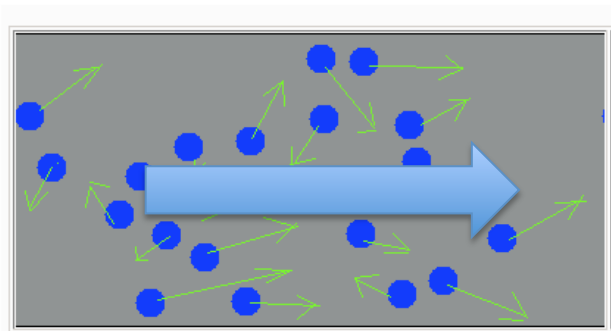


On average all the electrons are moving (drifting) to the right.

What is the direction of the field?

- A. to the right
- B. to the left
- C. up
- D. down

## Conductor in electric field



On average all the electrons are moving (drifting) to *the right*.

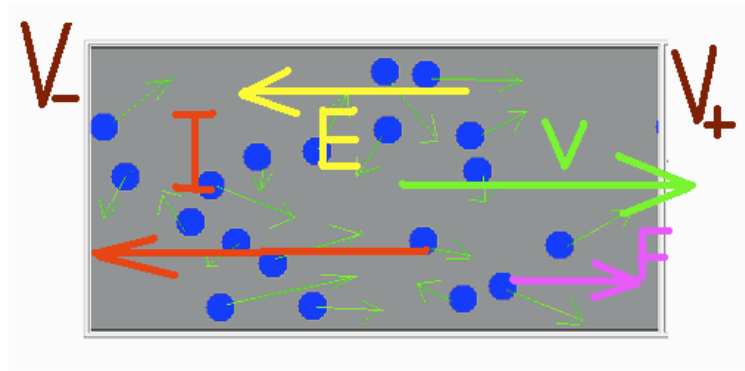
What is the direction of the field?

**B. to the left**

Electrons are negatively charged:  $\vec{F} = e\vec{E}$ ;  $e < 0$

If electrons on average are moving to the right, hence, the electrostatic force is acting to the right, hence the field is supposed to be directed *to the left*.

# Curent



Electric field  $E$  points to the left; it points from a high potential  $V_+$  to a low potential  $V_-$ .

Electric force on electrons  $F$  points to the right.

Average (drifting) velocity of electrons  $V$  points to the right.

Current  $I$  points to the left (in the direction of the field!).

(from a higher potential to a lower potential)

**(through a *passive* element!)**

## Current

Current is the rate of flow of charge. The symbol is I. The unit is the ampere (A), or amp for short.

$$\text{Amp} = \text{C/s}$$

$$I = \frac{\Delta Q}{\Delta t}$$

$$\Delta Q = I \Delta t$$

Although current in most cases consists of flowing electrons, the direction of the current on a circuit diagram is shown as the flow of positive charges.

How many electrons per second pass through a section of wire carrying a current of 2.10 A?

1.  $1.1 \times 10^{18}$  electrons/s

2.  $4.4 \times 10^{18}$  electrons/s

3.  $8.8 \times 10^{18}$  electrons/s

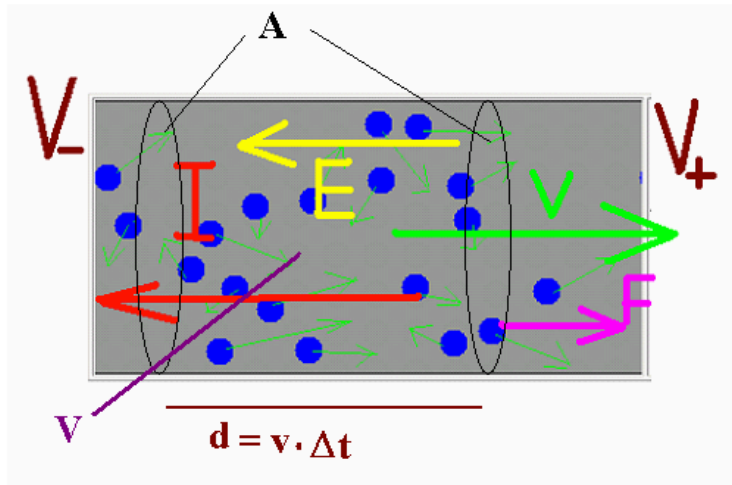
4.  $13.2 \times 10^{18}$  electrons/s

$$I = \frac{\Delta Q}{\Delta t} \rightarrow 2.1 = \frac{\Delta Q}{1s} \rightarrow \underline{\Delta Q = 2.1 C = N_e e}$$

$$I = \frac{Q}{t}$$

$$N_e = \frac{Q}{e} ;$$

# Current



(so many  $V$ 's!)

$$I = \frac{\Delta Q}{\Delta t}$$

$$\Delta Q = eN_e \quad N_e = V \cdot n$$

$V$  is the volume of the conductor between two cross-sectional surfaces;

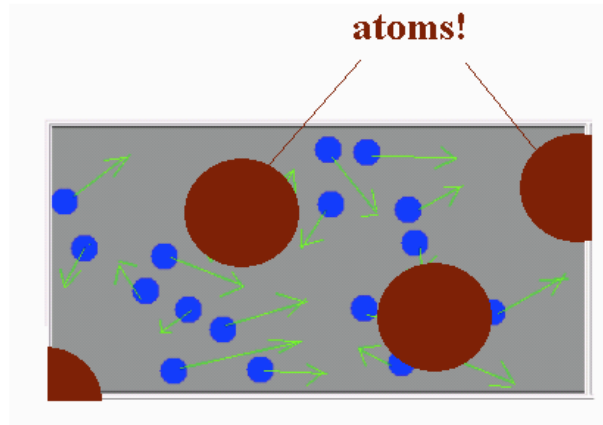
$n$  is the number electrons per  $m^3$  (density of electrons)

Volume  $V = A \cdot d$  and  $d = v \cdot \Delta t$  (velocity times time)  $\Rightarrow$

$$I = eAnv$$

To increase/decrease current we can increase /decrease cross-sectional area  $A$ ; or electron density  $n$ ; or drift velocity  $v$ .

# Nature of resistivity



What does prevent electrons from being constantly accelerated by the electric field?

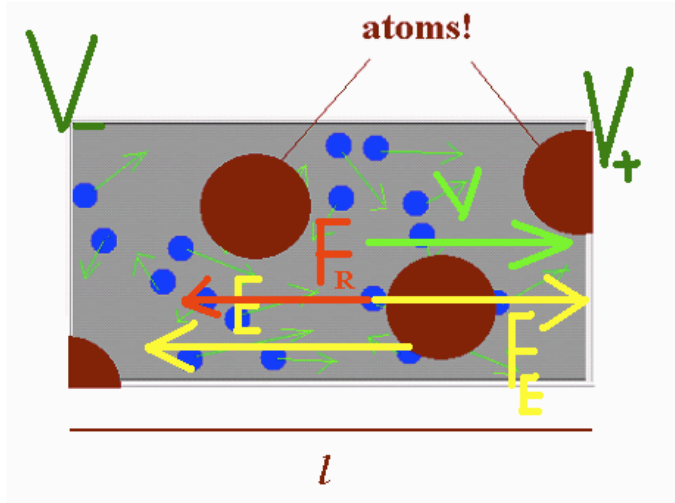
ATOMS!

Atoms provide a “frictional” force on electrons and slow them down.

**Current experiences resistive force,  
every wire has some resistance to current.**



## Current vs. Potential difference



$$I = eAnv$$

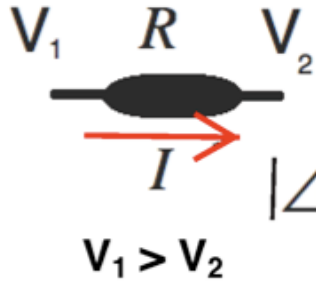
$$v = \beta^* F_R$$

$$F_R = e|\Delta V|/l$$

⇓

$$I = eAn\beta e \frac{|\Delta V|}{l} = e^2 n \beta \frac{A}{l} |\Delta V| = \frac{|\Delta V|}{R} = \frac{|\Delta V|}{\left(\rho \frac{l}{A}\right)}$$

# Ohm's Law, Resistance, Resistivity



$$|\Delta V| = V_1 - V_2 = IR$$

This is what we have proved:

$$I = \frac{|\Delta V|}{R} = \frac{|\Delta V|}{\left(\rho \frac{l}{A}\right)}$$

$$I = \frac{|\Delta V|}{R} \quad \text{or} \quad |\Delta V| = R I$$

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According to the Ohm's Law:

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*Resistance* of a wire is directly proportional to its length  $l$  and inversely proportional to its cross-sectional area  $A$  : the variable  $\rho$  is called *Resistivity* of the material (the metal the wire is

made of):

$$R = \rho \frac{l}{A}$$

$$R = \Omega \cdot m$$

### Resistivities<sup>a</sup> of Various Materials

Material	Resistivity $\rho$ ( $\Omega \cdot m$ )	Material	Resistivity $\rho$ ( $\Omega \cdot m$ )
<b>Conductors</b>		<b>Semiconductors</b>	
Aluminum	$2.82 \times 10^{-8}$	Carbon	$3.5 \times 10^{-5}$
Copper	$1.72 \times 10^{-8}$	Germanium	$0.5^b$
Gold	$2.44 \times 10^{-8}$	Silicon	20–2300 <sup>b</sup>
Iron	$9.7 \times 10^{-8}$	<b>Insulators</b>	
Mercury	$95.8 \times 10^{-8}$	Mica	$10^{11} - 10^{15}$
Nichrome (alloy)	$100 \times 10^{-8}$	Rubber (hard)	$10^{13} - 10^{16}$
Silver	$1.59 \times 10^{-8}$	Teflon	$10^{16}$
Tungsten	$5.6 \times 10^{-8}$	Wood (maple)	$3 \times 10^{10}$

<sup>a</sup> The values pertain to temperatures near 20 °C.

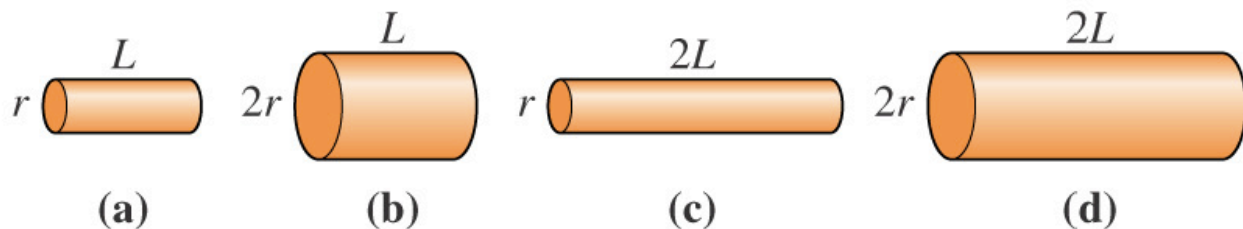
<sup>b</sup> Depending on purity.

$$R = \rho \frac{L}{A}$$

$$R = \rho \cdot \frac{1 \text{ m}}{1 \text{ m}^2}$$

Conductors a to d are all made of the same material. Rank in order, from largest to smallest, the resistances  $R_a$  to  $R_d$ .

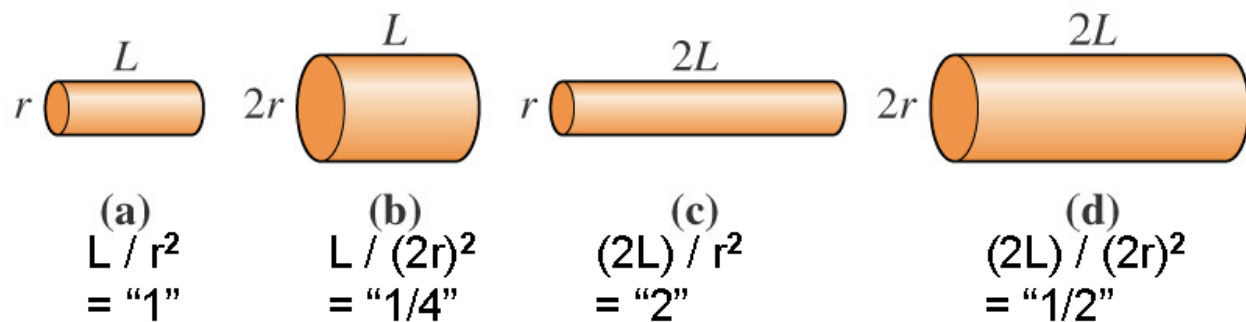
$$R = \rho \frac{L}{A}$$



1.  $R_a > R_c > R_b > R_d$
2.  $R_b > R_d > R_a > R_c$
3.  $R_c > R_a > R_d > R_b$
4.  $R_c > R_a = R_d > R_b$
5.  $R_d > R_b > R_c > R_a$



Conductors a to d are all made of the same material. Rank in order, from largest to smallest, the resistances  $R_a$  to  $R_d$ .

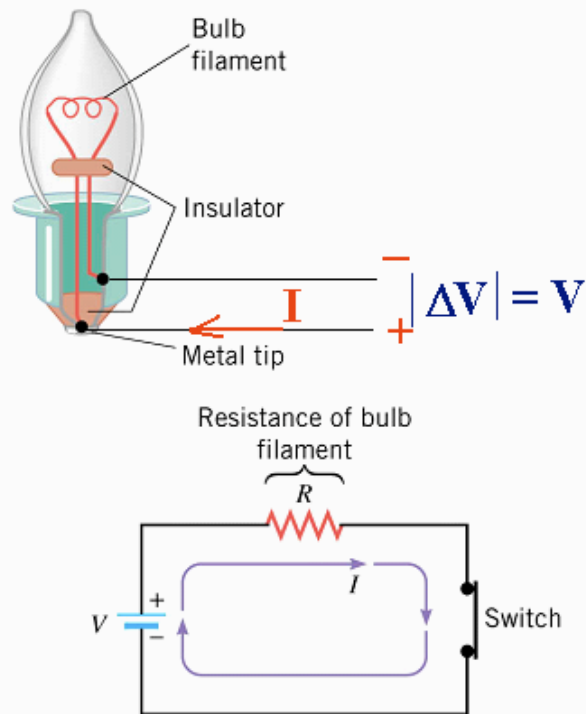


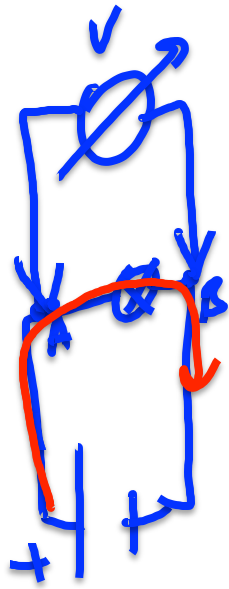
1.  $R_a > R_c > R_b > R_d$
2.  $R_b > R_d > R_a > R_c$
3.  $R_c > R_a > R_d > R_b$
4.  $R_c > R_a = R_d > R_b$
5.  $R_d > R_b > R_c > R_a$

## Flashlight

The filament in a light bulb is a resistor in the form of a thin piece of wire. The wire becomes hot enough to emit light because of the current in it. The flashlight uses two 1.5-V batteries to provide a current of 0.40 A in the filament. Determine the resistance of the glowing filament.

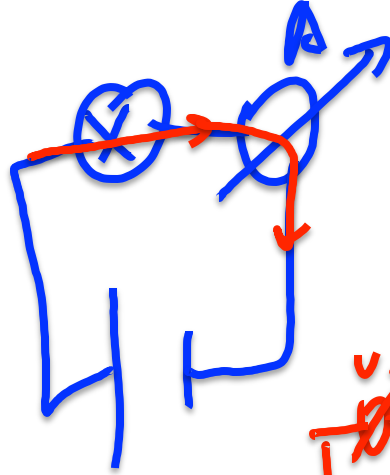
$$R = \frac{V}{I} = \frac{3.0 \text{ V}}{0.40 \text{ A}} = 7.5 \Omega$$



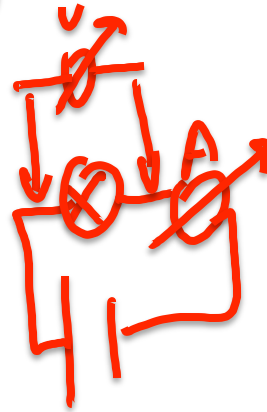


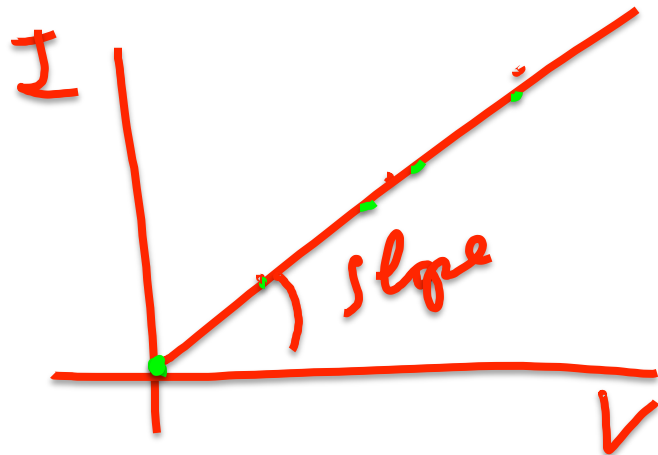
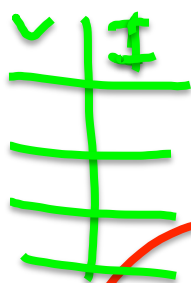
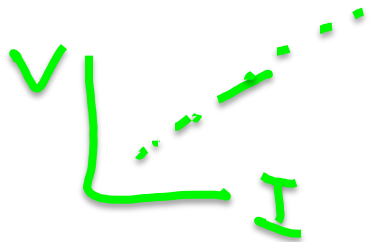
$$\underline{R_B = 0}$$

$$\underline{R_V = \infty}$$



$$\underline{R_A = 0}$$



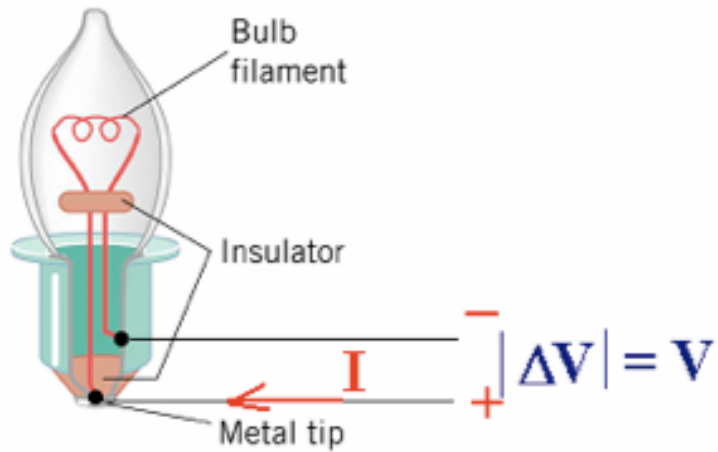


$$I = \frac{V}{R} = \left(\frac{1}{R}\right)V$$

$$Y = mX + b$$

- 1.  $R$
- 2.  $\frac{1}{R}$
- 3.  $\frac{V}{R}$
- 4. ?

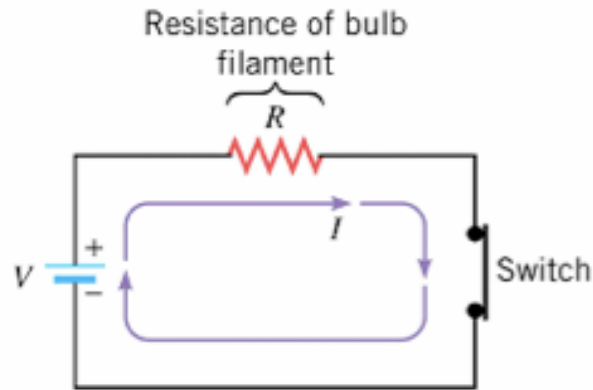


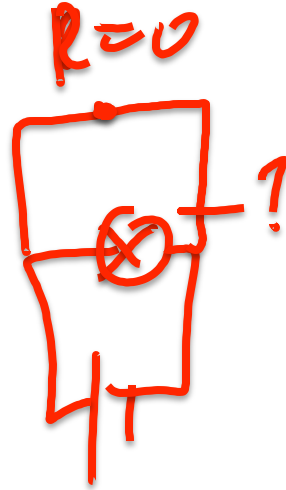
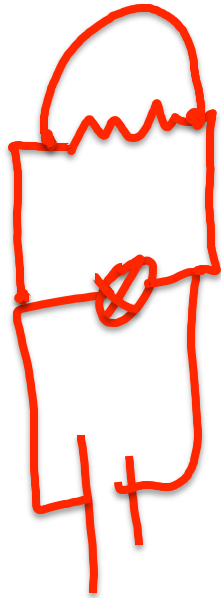


Due to electric current traveling through the filament of the bulb a flashlight is on.

Does the current do work?

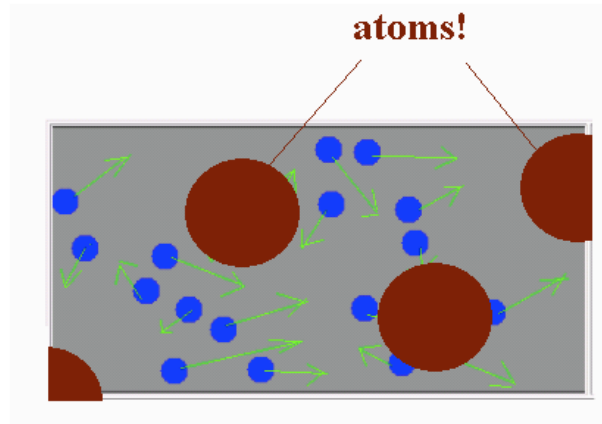
1. Yes
2. No





1. Nothing
2. Brighter
3. Dimmer

# Work of an electric current



When moving through a conductor, electrons constantly encounter atoms and hit them making atoms moving/shaking faster!

Potential difference create electric field  $\Rightarrow$  E field creates a force on electrons making them moving creating current  $\Rightarrow$  E field does a work on electrons  $\Rightarrow$  electrons hit atoms  $\Rightarrow$  electrons transfer energy to atoms  $\Rightarrow$  electrons do work on atoms  $\Rightarrow$  current does work on atoms  $\Rightarrow$

**current does work!**